

Linear Inequalities

Recall:

Open circle = NOT equal to


closed circle = equal to

Now in two variables

Instead of an open circle, we have an open line (dashed).

Instead of a closed circle, we have a closed line (solid).

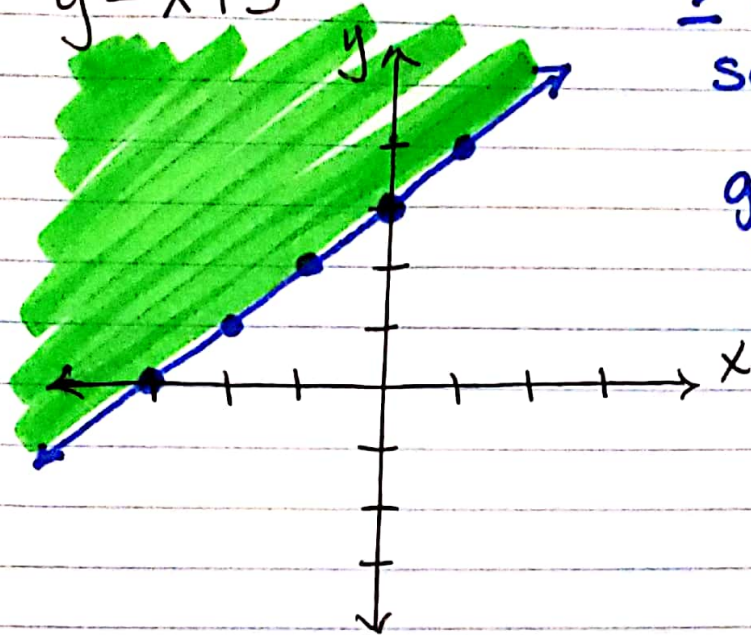
In two variables we shade w/ respect to y .

y -axis = vertical = 

For $>$ and \geq we shade up
(above the line)

For $<$ and \leq we shade down
(below the line)

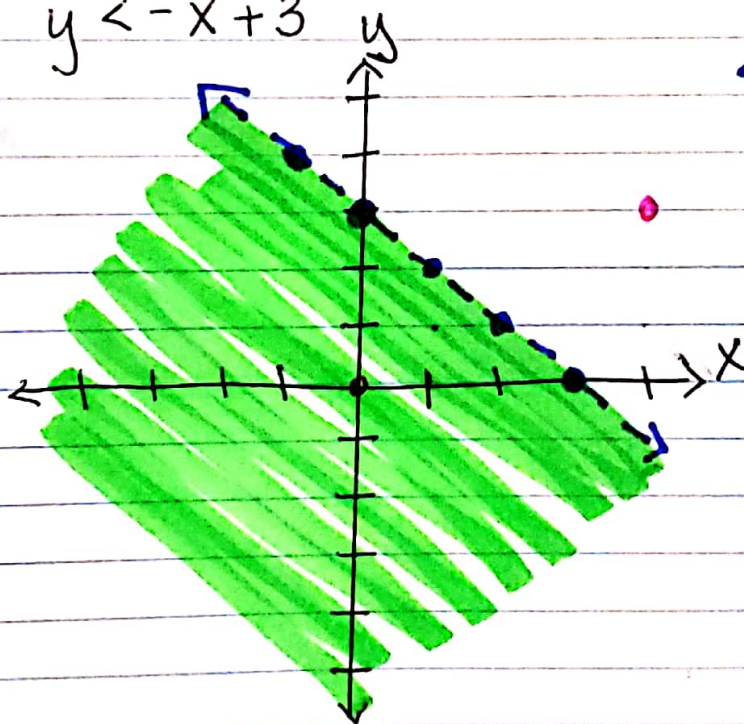
Slope: $m=1$ \swarrow y-int
Ex: $y \geq x+3$



\geq = equal to
solid line

greater than y
shade up

Slope: $m=-1$ \swarrow y-int
Ex: $y < -x+3$



$<$ = NOT equal
dashed line

less than y
shade
down

Is $(0,0)$ part of the solution? Yes

Is $(4,3)$ part of the solution? NO

Is $(0,3)$ part of the solution? NO

Writing, Solving, and Graphing Linear Inequalities

Write an inequality based on each given scenario. **Solve** the inequality. **Graph** the inequality.

1. You receive an \$80 gift card to the bookstore. Hardback books cost \$8 and paperback books cost \$4. How many books of each type can you buy?

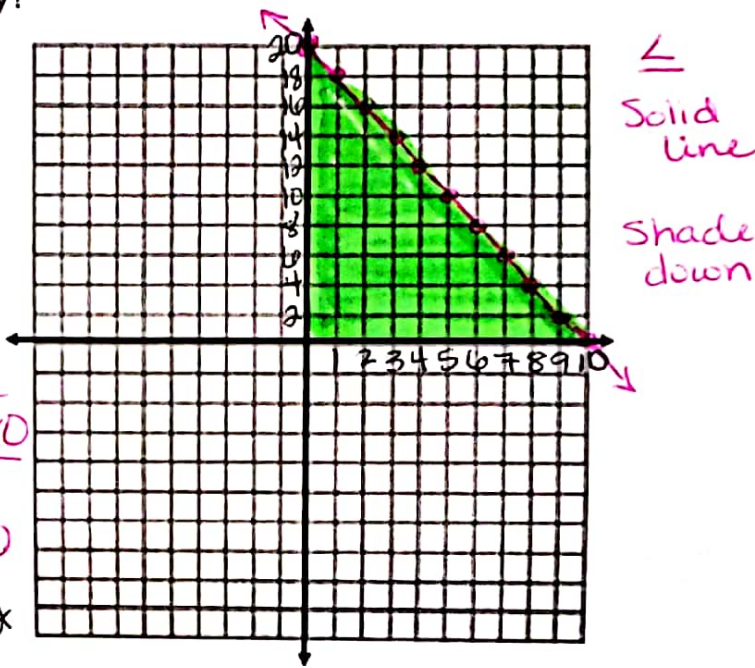
Inequality: $8x + 4y \leq 80$

Solution: $y \leq -2x + 20$

Hardback = x
Paperback = y

$$\begin{array}{r} 8x + 4y \leq 80 \\ -8x \qquad -8x \\ \hline 4y \leq -8x + 80 \\ \frac{4y}{4} \leq \frac{-8x + 80}{4} \\ y \leq -2x + 20 \end{array}$$

slope $m = -2$ y -int



2. A catering company has small tables and large tables. Small tables seat 4 people and large tables seat 6. They are planning a party for ¹⁰⁰₁₅₀ guests. How many of each size table can they use?

Inequality: $4x + 6y \leq 150$

Solution: _____

Small - x
Large - y

$$\begin{array}{r} 4x + 6y \leq 150 \\ -4x \qquad -4x \\ \hline 6y \leq -4x + 150 \\ \frac{6y}{6} \leq \frac{-4x + 150}{6} \\ y \leq -\frac{2}{3}x + 25 \end{array}$$

$y = -\frac{2}{3}(3) + 25$
 $y = -2 + 25$
 $y = 23$

$y = -\frac{2}{3}(6) + 25$
 $y = -4 + 25$
 $y = 21$

